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BEFORE COMPLETING FORM REPORT DOCUMENTATION PAGE 2. GOVT ACCESSION NO. 3. RECIPIENT'S CATALOG NUMBER A 09 HDL-TR-1931 A Near-Surface Burst EMP Driver Package Technical Repet for Prompt Gamma-Induced Sources & PERFORMING ORG. REPORT NUMBER · AUTHOR(4) CONTRACT OR GRANT NUMBER(+) William T./Wyatt, Jr $\mathscr S$ DA: \ 1L16212ØAH25 . PERFORMING ORGANIZATION NAME AND ADDRESS Harry Diamond Laboratories 2800 Powder Mill Road Adelphi, MD 20783 Prog. El.: 6.21.20.A 1. CONTROLLING OFFICE NAME AND ADDRESS REPORT DATE U.S. Army Materiel Development and Readiness Command UNCLASSIFIED 15a, DECLASSIFICATION/DOWNGRADING 16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited. 17. DISTRIBUTION STATEMENT (of the abstract entered in Black 20, If different from Report) 18. SUPPLEMENTARY NOTES HDL Project: X750E6 DRCMS Code: 612120.H250011 19. KEY WORDS (Continue on reverse side if necessary and identity by block number) Curve fitting Electromagnetic pulse Compton currents Radiation transport Nuclear explosions Monte Carlo method Gamma rays Computer codes ASSTRACT (Continue on reverse side if recovery and identity by block number) This report summarizes the development of a software package specifying electromagnetic pulse (EMP) drivers produced by prompt gamma rays emitted by a near-surface nuclear burst in the air. The package is designed for use with the NEMP EMP prediction computer code. This report describes improved calculations of EMP drivers arising from a point gamma source in air over ground, based on Monte Carlo simulation of the gamma transport by the specially

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20. Abstract (Cont'd)

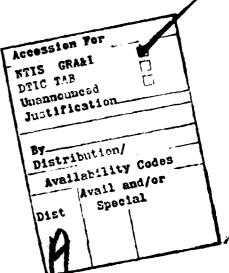
developed SLEDGE computer code. This simulation was done for seven source gamma energies from 0.5 to 7.0 MeV. The transport was carried to a range of 25 mean free paths. Correlated sampling was used to estimate Compton electron currents more accurately. The theoretical basis of the SLEDGE code is discussed. Analytic approximations to the Monte Carlo results are described in detail, including (1) the energy deposition buildup factor (both free field and ground influenced), (2) time dependence of energy deposition as a function of both range from the burst and nearness to the ground, (3) ratio of radial Compton electron current to energy deposition rate, and (4) theta Compton electron current due to the presence of the ground. Comparisons are made with two previous EMP driver packages, with good agreement for cases where the previous packages are believed reliable.

FOREWORD

The nuclear electromagnetic pulse (EMP) is a transient broadband electromagnetic field capable of damaging or upsetting electronic equipment on the tactical nuclear battlefield. To predict the signature of the EMP generated by a nuclear burst, it is necessary to determine the EMP drivers—time and space varying ionization and Compton electron currents in the nuclear radiation field around the burst. Once the ionization and Compton currents are specified, it is usually possible to solve some form of Maxwell's equations for the EMP generated.

This report summarizes the development of a software package specifying EMP drivers produced by prompt gamma rays emitted by a near-surface burst in the air. The package was designed for use with the NEMP EMP environment prediction computer code used at the Harry Diamond Laboratories. A separate report, A Near-Surface Burst EMP Driver Package for Neutron-Induced Sources, HDL-TR-1930 (September 1980), summarizes the development of a similar software package for EMP drivers due to neutrons and neutron-induced secondary gamma rays.

Part I of this report describes the development of the Monte Carlo gamma ray transport computer code and data base to be fitted. Part II describes the curve-fitting exercise and compares these results with earlier results.



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PART I. EMP DRIVERS FROM GAMMA TRANSPORT BY MONTE CARLO

1. REQUIREMENTS FOR NEW EMP DRIVER AND GAMMA TRANSPORT DATA

Electromagnetic pulse (EMP) drivers consist of one component arising from prompt gamma radiation and a second component arising from neutron radiation. The NEMP computer code^{1,2} obtains the solution of Maxwell's equations for EMP from a near-surface burst in the air. The EMP drivers must be incorporated into the NEMP code as smooth fits to quasi-analytic or Monte Carlo predictions. Earlier EMP driver fits were used in the LEMP computer code³ for EMP from surface bursts. The LEMP prompt gamma ray EMP drivers were used in the NEMP code at first, but a quick-look Monte Carlo study by this author confirmed several deficiencies in these LEMP drivers:

- a. Incorrect range dependence for the gamma ray buildup factor at more than about five gamma ray attenuation lengths penetration, becoming exponentially worse at deeper penetrations
- b. Incorrect time dependence at deeper penetrations (LEMP drivers' time dependence is independent of range and decreases with time too rapidly at deeper penetrations.)
- c. Lack of a ground effect on the buildup factor (The ground actually inhibits the increase of the buildup factor with range for observers near the ground.)
- d. Lack of late vertical Compton currents induced by the effect of the ground on gamma transport

It was therefore decided to develop newer, more realistic drivers for the NEMP code that would overcome these deficiencies and also account for the effect of a nonzero burst height. The new drivers would be valid to a penetration depth of at least 20 gamma ray attenuation lengths and would encompass more discrete gamma ray energies than the LEMP drivers (which included 0.5-, 1.5-, and 5.0-MeV gamma ray sources). The new drivers would use the same LEMP philosophy of using well-chosen analytic functionals to describe time and space dependence of the data, in preference to using piecewise polynomial fits.

¹H. J. Longley, C. L. Longmire, and K. S. Smith, Development of NEMP (U), Mission Research Corp., Santa Barbara, CA, HDL-CR-75-001-1 (April 1975). (SECRET--RESTRICTED DATA)

²H. J. Longley and K. S. Smith, Developments in NEMP for 1977 (U), Mission Research Corp., Santa Barbara, CA, HDL-CR-77-0022-1 (January 1978). (SECRET--RESTRICTED DATA)

³H. J. Longley and C. L. Longmire, Development and Testing of LEMP 1, Los Alamos Scientific Laboratory, NM, LA-4346 (April 1970).

2. DEVELOPMENT OF SLEDGE, A MONTE CARLO GAMMA TRANSPORT CODE

To first test the validity of the LEMP drivers and then obtain needed, more detailed predictions of EMP drivers, it was decided to write a special-purpose Monte Carlo code for gamma ray transport, specially tailored for efficiency in calculating the data needed. The code was written in FORTRAN IV and run on the Harry Diamond Laboratories (HDL) computer (an IBM System/370 Model 168). The code consists of several thousand FORTRAN statements and includes 53 program and subprogram units. It was named SLEDGE, after the basic tool for realigning existing structures; "SLEDGE" is also an acronym for "surface and low-altitude EMP drivers due to gamma emission." An overview of the SLEDGE code is presented here with additional detail on innovations or other important aspects.

The SLEDGE code models time-dependent gamma ray transport from a point source in air-over-ground cylindrical geometry. The collision kernel includes Compton scattering, photoabsorption, and pair production. Time dependence is maintained in retarded time from the source point (the nuclear burst). For this study, the gamma ray source was monochromatic in energy and a delta function in time.

The gamma ray flux is sampled to obtain the desired EMP driver response functions—electron current vector and energy deposition rate. Energy deposition and radial and theta components of the electron current vector are scored within volume detectors by both track-length and collision estimators of the gamma ray flux and are scored at the surfaces of volume detectors by a boundary crossing estimator of the gamma ray flux. Optionally, collision estimator scoring can be done in spherical polar coordinate radial bins to obtain one-dimensional (1-d) results. Thus, removal of the ground allows spherically symmetric free-field results to be accumulated in the 1-d radial bins. Inclusion of the ground allows azimuthally symmetric, ground—influenced results to be accumulated in the 2-d cylindrical geometry volume detectors.

The random walk permits exponential transform biasing, angular and energy biasing of the source, and directional biasing of gamma rays emerging from Compton collisions. Splitting can be done to prevent growth of particle weight due to biasing at collisions or at transports. Splitting and roulette can be used in connection with detector importances to improve statistics in desired regions (zone splitting). Splitting and roulette can be used also to reduce the variance of gamma ray weights in specifiable detectors (weight balancing). A special technique may be used to greatly reduce the variance of the ratio of electron current to energy deposition rate, based on the (early time) correlation between the electron currents and the energy deposition.

2.1 Random Walk and Estimator Scoring

After reading problem input, setting up time and space meshes, and initializing necessary tables, the SLEDGE code executes a batch loop and then scans the results of each batch to develop grand totals and batch statistics. Each batch consists of a particle (gamma ray) history loop followed by saving the total results for the batch. A typical production run of 30,000 histories might consist of 20 batches of 1500 histories each. Each particle history consists of identifying a particle and all its subparticles created by splitting and following them through successive random walks until extinction. The random walk consists of these steps:

- (1) Generating the particle or subparticle
- (2) Determining the number of mean free paths down which the particle is to be transported prior to a collision
- (3) Tracking the particle through space and time to the collision point, while scoring track-length or surface crossing estimators for the detectors encountered
- (4) Colliding the particle to obtain the emergent particle energy and direction, while scoring collision estimators for the detector involved, and then repeating steps (2), (3), and (4) until extinction

The particle or subparticle can be killed or split after step (2) or (3) or (4) through photoabsorption, escape, age cutoff, low energy cutoff, collision number limit, or any of the roulette or splitting mechanisms. Subparticles produced are stored in a split stack and are withdrawn one at a time from the split stack in step (1). Ultimately, there are no entries remaining in the split stack, and the next particle history can be started.

Many standard techniques were drawn from the literature, particularly from Carter and Cashwell. $^{\rm L}$

Generating the particle involves determining its position (at the burst), direction cosines (usually biased), energy (simply monochromatic in this study), age, and weight.

Determining the number of mean free paths, N, was done by

$$N = - \ln (\xi)$$

⁴L. L. Carter and E. D. Cashwell, Particle-Transport Simulation with the Monte Carlo Method, U.S. Energy Research and Development Administration TID-26607 (1975).

for a uniform random number, ξ , selected from the interval (0,1). A rejection method was used to eliminate escapes before the first scatter for a particle. Both exponential transform and importance function biasing were used for first-scatter transport, and exponential transform biasing was used for later scatters. These are discussed in more detail in section 2.2.

Tracking the particle involved finding its track-length in the detector that it was inside (detector volumes being mutually exclusive and filling all space within the grid outer boundary), scoring track-length and surface crossing estimators, moving the particle to the next detector, and repeating the process until the particle reached a collision point or was killed. When the particle reached a collision point, the 2-d and 1-d collision estimators were scored, also.

Standard means were used to select the collision event from Compton collision, photoabsorption, and pair production probabilities. Pair production was assumed isotropic. Standard algorithms were used to select the emergent energy and the direction of Compton scattered gamma rays. Emergent direction biasing could be used, as described in section 2.2.

The track-length estimation of the flux, F (that is, path length per unit volume), is

$$F = pW_{BC}/V$$
,

where p is the track-length in the particular volume detector and time bin, W_{BC} is the particle weight before collision, and V is the detector volume. The electron current magnitude, J, is

$$J = F \left(R_C / \lambda_C + R_p / \lambda_p \right) ,$$

where ${\rm R_C}$ is the average forward range of Compton electrons (for the incident gamma ray energy), λ_C is the Compton collision or attenuation length, ${\rm R_P}$ is the average forward range of photoelectrons, and $\lambda_{\rm P}$ is the photoelectric absorption length. ${\rm R_C}$ was computed and tabulated by the SLEDGE code by using the Compton differential scattering cross section and the electron range-energy relation in air. ${\rm R_P}$ was adapted from the literature. The energy deposition, D, is

$$D = F \left[E/\lambda_a + E/\lambda_p + (E - 1.022)/\lambda_{pp} \right] ,$$

where E is the gamma ray energy in MeV, λ_a is the Compton absorption length, and λ_{pp} is the pair production absorption length.

Once ${\tt J}$ is obtained, it is decomposed into radial and vertical components.

The surface crossing estimation of the flux, scored only when the surface is crossed, is

$$F = W_{BC}/CA$$
,

where C is the sine of the angle between the surface and the particle direction and A is the area of the surface. J and D are derived as before.

The collision estimation of the flux, scored only when a collision point is reached, is

$$F = W_{BC}/\sigma V$$
,

where σ is the total collision cross section in the detector with volume V_{\bullet} J and D are derived as before.

The time bin associated with scoring surface crossing and collision estimators is simple to determine. However, for the track-length estimator, the particle may pass through several time bins while traversing a detector volume. The portion of the track-length spent in each time bin must be determined to score the time dependence properly. Although this determination requires somewhat more computer time, the associated variance is usually much better for the track-length estimator. Generally, all three estimators were used to check for agreement and insure correct results.

No account was taken of the effect of the ground upon the transport of Compton electrons and photoelectrons. Some effects would be expected within roughly 1 m of the ground. This effect could be a fruitful subject for future study.

2.2 Biasing and Importance Functions

The analog model of gamma ray transport (that is, no biasing or importance functions) is useless for deep penetration problems. Some means must be used to force gamma rays to penetrate to distant regions in large enough numbers to produce useful, low variance results. A number of methods were tested in the SLEDGE code for the problems under consideration. These may be categorized as (1) source biasing, (2) transport biasing, and (3) collision biasing, modifying respectively the source function, the transport kernel, or the collision kernel of the transport integral. Two risks are associated with the use of properly normalized biasing methods:

a. The variance of the flux may be infinite or possibly very large so that as the number of batches increases, the variance gets larger, not smaller.

b. The transport integral (integrated over position, velocity, time, and energy) may be undersampled since strong biasing may force the sampling away from portions of the integral space that contribute significantly to the correct answer.

Thus, the biasing methods must be properly constructed and not overused and yet must be powerful enough to be worth the trouble of using. In general, source biasing very effectively reduces the variance in deep penetration problems. Also, splitting with roulette is a simple but highly effective method for transport biasing. In this study, collision biasing was only of minor importance in variance reduction.

2.2.1 Source Biasing

Source directional biasing was not used in the SLEDGE code to obtain 1-d results. However, for the 2-d air-over-ground studies, source directional biasing was used by construction of a cumulative distribution function (cdf) based on a nonisotropic importance function. Conventional cylindrical coordinates (ρ,z,ϕ) are used, where z is positive upward. If the particle direction cosine, x, is

$$x = z/(\rho^2 + z^2)^{1/2},$$

then the probability density function (pdf), which describes an isotropic source angular distribution, is

$$p(x) = 1/2, -1 \le x \le 1$$
.

A suitable anisotropic pdf, which biases the selection toward certain target direction cosines \mathbf{x}_i , is

$$p(x) = A \sum_{i=1}^{N} \left\{ 1 + \beta_i / \left[1 + \beta_i (x - x_i)^2 \right] \right\}$$

where A normalizes p(x) to have an integral of unity (taken from x=-1 to x=1) and where β_i and x_i are N bias strengths and bias directions. If a β_i is zero, there is no bias toward the corresponding x_i ; if all β_i are zero, the pdf is isotropic. The associated cdf is

$$c(x) = \int_{-1}^{x} p(x') dx'.$$

and the scattering direction is obtained in the usual way by selecting a random number, ξ , from the uniform distribution on (0,1) and then solving

$$c(x) = \xi$$

for x. The associated weight is simply 1/p(x).

The transport to the first collision was included as part of the source biasing and treated separately from subsequent transport biasing. In addition to the directional biasing already described, two types of path length biasing were used: (1) the well-known exponential transform and (2) an importance function. The exponential transform is not described further since it is a standard technique. For the importance function, instead of sampling from a simple exponential distribution, $e^{-\alpha r}$, in the transport integral

where α is the range attenuation coefficient, we wish to sample from the distribution

$$(1 + \gamma r)e^{-\eta r}$$
,

where γ is an additional parameter and η is a different attenuation coefficient. Typically, η may be an order of magnitude smaller than α to achieve deep penetration by the first scatter, and γ may be about unity. If γ is zero, the importance function reduces to the exponential transform, while if γ is about unity, the deep penetration statistics are markedly improved over the simple exponential transform. Since gamma ray buildup factors are roughly proportional to r, the γr factor actually suffices to compensate for $1/r^2$ geometric attenuation. A rejection method also was used to eliminate escapes before the first collision.

2.2.2 Transport Biasing

Several methods of biasing the transport kernel were used. A directional exponential transform was sometimes used to force longer transports in the outer direction, but was found unnecessary when region weight balancing and region importances were used with splitting and roulette.

Weight balancing involved keeping the particle weights near an optimum weight, which was a function of the distance from the burst. As necessary, particle weights were adjusted after each collision by splitting or playing roulette. Keeping the weights nearly the same within a volume detector caused the mean square weight to be close to the mean weight, leading to improved statistics. The optimum weight was the first collision weight multiplied by the approximate buildup factor,

$$w_{opt} = B(r)wl(r)$$
,

where B(r) is the approximate buildup factor at range r from the burst and $w_l(r)$ is the first-collision weight at range r. If no source transport bias were used, weight $w_l(r)$ of a particle undergoing a first

collision at range r would be unity for all r. However, the use of the importance function described in section 2.2.1 causes weight w1 to be a function of r.

Region importances also were implemented. Various regions were assigned numerical ratings of their importance by the input to the SLEDGE code. For example, detectors near the ground were more important than detectors far above the ground. When a particle passed from a region of less importance to a region of greater importance, it was split. When passing the other way, roulette was played. Thus, more particles were tracked in more important regions, and fewer were tracked in less important regions.

2.2.3 Collision Biasing

In several problems, it was found helpful to use collision biasing, in which the emergent particle direction (scattering direction) was biased toward one or more areas of particular interest. The scattering direction was biased only for Compton scattering. For photoabsorption, the gamma ray is completely absorbed. For pair production, the scattering directions of the two locally produced annihilation quanta were assumed to be isotropic and opposite to each other. For Compton scattering, the bias importance function used was

$$I_{c} = \sum_{i=1}^{M} 1/\left[1 - \kappa_{i}(\hat{r} \cdot \hat{r}_{i})\right] ,$$

where

 κ_i is the bias strength in the ith bias direction, \hat{r} is the unit vector in the scattering direction, \hat{r}_i is the unit vector in the ith bias direction.

The dot product $\hat{r} \cdot \hat{r_i}$ is the cosine of the angle between \hat{r} and $\hat{r_i}$ so that I_c is maximized when \hat{r} and $\hat{r_i}$ are parallel.

Construction of a properly normalized pdf based on importance function $\mathbf{I}_{\mathbf{C}}$ can be awkward, because the complete angular integral,

$$Q = \int_{4\pi} d\Omega \ I_{c} \sigma_{c}(\phi, \theta) \ ,$$

is required, where $\sigma_{\rm C}(\phi,\theta)$ is the Compton differential scattering cross section. Since $\sigma_{\rm C}(\phi,\theta)$ is not a simple function, the integral cannot be obtained analytically. A numerical integration would be time-consuming. Even a straightforward rejection method requires the same

integral to conserve particle weight. Hence, a special algorithm was devised to allow use of the rejection method to implement $\mathbf{I}_{\mathbf{C}}$. The algorithm uses recursive binary splitting with roulette to obtain exactly one surviving particle. The algorithm conserves weight and has a low variance. Briefly, the algorithm consists of the following steps to obtain the biased scattering direction, Ω , for a particle of weight, W:

- (1) Select roulette variable V uniformly from the set (1,2).
- (2) Generate random trial scattering direction Ω_l for a first split and get rejection probability R_l .
- (3) Test for rejection of the first split. If it is rejected, set W = W/2 and return to step (2).
- (4) Otherwise, generate random trial scattering direction Ω_2 for a second split and get rejection probability R_2 .
- (5) Test for rejection of the second split. If it is rejected, set $W = W/(2 2/R_1)$, set $\Omega = \Omega_1$, and go to Finish.
- (6) Otherwise, if V=1, set $W=W/(1-R_1)$, set $\Omega=\Omega_1$, and go to Finish.
- (7) Otherwise, if V=2, set $W=W/(1-R_2)$, set $\Omega=\Omega_2$, and go to Finish.

Finish This is the end of the algorithm.

This algorithm allows the use of the rejection method without the need to evaluate normalization integral Q.

In a number of SLEDGE runs, this algorithm was successfully used to push particles away from the ground and toward certain volume detectors with poor statistics.

2.3 Cross Sections

The well-known Klein-Nishina expressions were used for the Compton scattering cross section. For the media under consideration (air and ground), the Compton cross section dominates cross sections for photoabsorption and pair production over a wide energy range.

The attenuation coefficient for pair production was approximated by the simple expression

$$\tau_{\rm pp} \simeq 1.84 \times 10^{-4} \rho \bar{z}^2 (\hat{E} - 0.014 \hat{E}^2) / \bar{A},$$

where

 τ_{pp} is in inverse centimeters,

is the material density in grams per cubic centimeter,

 \overline{z}^2 is the mean square atomic number of the material,

 $\hat{\mathbf{E}}$ is E - 1.022, and E is the gamma ray energy in MeV,

A is the mean atomic weight of the material.

For air, $\bar{Z}^2 = 106.4$ and $\bar{A} = 28.9$.

For aluminum, $\bar{Z}^2 = 13^2$ and $\bar{A} = 27.0$.

The attenuation coefficient for photoabsorption was approximated by

$$\tau_{\rm ph} \simeq \frac{1.88 \times 10^{-2} \rho \bar{z}^4}{\bar{\lambda}(100E)^{3.49-0.0035(\log \bar{z}^4)^2}}$$

where the logarithm is to the base 10. The material mean fourth power of the atomic number is 6.46×10^3 for air and 13^4 for aluminum. This approximation has no significant error for air, but is about 10 percent low for aluminum.

The error incurred in the total absorption cross section by using these approximations appears to be less than 1 percent in air for gamma ray energies from 0.01 to 10 MeV. The error in aluminum is slightly greater for energies less than 0.1 MeV. The values for aluminum are cited here because the air-over-ground transport studies were done over an aluminum ground for simplicity. The gamma ray cross-section properties of aluminum are similar to a typical ground composed of silicon, aluminum, oxygen, and water.

2.4 Scoring EMP Drivers by Correlated Sampling

A particularly useful innovation in the SLEDGE code concerns exploitation of the correlation between the energy deposition response function and the (Compton and photoelectric) electron current response function. When EMP drivers are scored, the electron current contribution is found to be correlated with the associated energy deposition contribution. The correlation is high at early times when the gamma ray direction is well collimated, but becomes low at later times when the gamma ray direction is poorly collimated. Ultimately, the correlation drops to zero as the many scatters produce an isotropic gamma direction. The correlation can be exploited in the following way.

Define the energy deposition score in a volume detector, k, and time bin, ℓ ,

$$\mathbf{s}_{\mathbf{k}l} = \frac{1}{n} \sum_{\mathbf{m}=1}^{n} \mathbf{s}_{\mathbf{k}l\mathbf{m}}$$

and the radial (for example) electron current as

$$J_{k\ell} = \frac{1}{n} \sum_{m=1}^{n} j_{k\ell m} ,$$

where m denotes the batch number of a total of n batches. Thus, $s_{k\ell m}$ is the energy deposition score for the kth detector, ℓ th time bin, and mth batch. Define also arbitrary function $H_{k\ell}$, which depends on the detector and the time bin. Consider the variance of the linear combination $J_{k\ell} - H_{k\ell} S_{k\ell}$:

$$VAR \left\{ J_{k\ell} - H_{k\ell} S_{k\ell} \right\} = \sum_{m} j_{k\ell m}^2 - 2H_{k\ell} \sum_{m} j_{k\ell m} s_{k\ell m} + H^2_{k\ell} \sum_{m} s_{k\ell m}^2 .$$

If $j_{k\ell m}$ and $H_{k\ell}s_{k\ell m}$ are positively correlated, the negative term on the right hand side reduces the variance; if the correlation coefficient of $j_{k\ell m}$ and $H_{k\ell}s_{k\ell m}$ is unity, the right hand side becomes zero. Therefore, on the assumption that $j_{k\ell m}$ and $H_{k\ell}s_{k\ell m}$ are at least partly correlated, solve the equation

for $\mathbf{H}_{\mathbf{k}\ell}$ by least-squares regression. This regression value for $\mathbf{H}_{\mathbf{k}\ell}$ should minimize

$$VAR \left\{J_{k\ell} - H_{k\ell}S_{k\ell}\right\}$$

and make optimum use of any correlation between jklm and Hklsklm.

In practice with the SLEDGE code, this correlated sampling technique improved the electron radial current fractional deviation statistics by more than an order of magnitude, except at later times when all remaining gamma rays have been scattered many times. The electron theta current statistics were similarly improved by more than a factor of two, especially at late times when significant theta currents were developing.

3. CALCULATIONS PERFORMED

3.1 One-Dimensional Studies

The principal aspects of gamma ray transport can be described in terms of buildup factors. (A buildup factor for an effect is the ratio of the effect as engendered by uncollided and multiply scattered gamma ray flux, to the effect as engendered by uncollided gamma flux.) The SLEDGE code was run for seven discrete gamma ray energy sources (table 1) in a homogeneous free air geometry. Results for the time integrated energy deposition buildup factor were obtained from 25 1-d radial bins, each 1 attenuation length wide, extending to a maximum range of 25 attenuation lengths. Fractional deviations varied from about 3 percent at the closer radial bins to about 10 percent for the most distant. For each gamma ray energy, a SLEDGE run was made consisting of 25 batches of 4000 histories each, for a total of 100,000 histories. A typical run tallied about one million collisions (scatters) and consumed about 40 min of central processing unit (CPU) time on the HDL computer (an IBM 370/168). Results were stored on magnetic tape for subsequent analysis and curve fitting.

TABLE 1. SEVEN GAMMA RAY ENERGIES AND ATTENUATION PARAMETERS

Source gamma ray energy (MeV)	Total attenuation coefficient (m ⁻¹)	1 attenuation length (m)	25 attenuation lengths (m)	
0.5	0.009604	104.12	2603.08	
1.0	0.007014	142.57	3564.30	
1.5	0.005734	174.40	4359.96	
2.5	0.004377	228.47	5711.67	
3.5	0.003651	273.90	6847.44	
5.0	0.003034	329.60	8239.95	
7.0	0.002596	385.21	9630.20	

Table 1 lists the total attenuation coefficient and distances corresponding to 1 and 25 attenuation lengths. An air density of $1.11 \times kg/m^3$ is assumed.

Time-dependent results also were obtained from these studies. The time bin structure used was the same as for the 2-d problems, shown in table 2.

TABLE 2. SLEDGE MESHES FOR TWO-DIMENSIONAL PROBLEMS

Time bin boundaries (s)	Radial boundaries (m)	Vertical boundaries (m)
0.00	0.0	-1.0
5.00(-9) ^a	300.0	0.0 ^b
1.00(-8)	600.0	25.0
2.00(-8)	900.0	50.0
3.25(-8)	1200.0	100.0
5.00(-8)	1500.0	200.0
7.50(-8)	1800.0	400.0
1.00(-7)	2100.0	600.0
1.50(-7)	2400.0	3000.0
2.00(-7)	2700.0	
3.00(-7)	3000.0	
4.00(-7)		
6.00(-7)		
1.00(-6)		
1.50(-6)		
2.00(-6)		
3.00(-6)		
5.00(-6)		
1.00(-5)		

^aRead as 5.00×10^{-9} .

3.2 Two-Dimensional Air-Ground Interface Effects

The 2-d air-over-ground gamma ray transport problem may be considered as a perturbed free-field problem. Significant perturbations are expected near the air-ground interface. The SLEDGE code was run for a 1.5-MeV gamma ray source in a cylindrical air-over-ground geometry. A burst height of 200 m was used. As mentioned in section 2.3, the ground was assumed for simplicity to be aluminum, whose gamma ray cross-section

 $^{^{}b}$ Air-ground interface at 0.0-m height.

properties are analogous to a typical ground composed of silicon, aluminum, oxygen, and water. The radial (horizontal) mesh extended to a 3000-m ground range, and the vertical mesh extended to a 3000-m height aboveground and to a 1-m depth belowground. Eighteen time bins were used, extending to a 10-µs retarded time. These grids are shown in table 2. Correlated sampling was used for the radial Compton current, but not for the theta Compton current. Various biases and importance functions were used, as described in section 2.2. The run consisted of 30 batches of 20,000 histories each, for a total of 600,000 histories. In longer than 2 hr of CPU running, nearly four million collisions (scatters) were tallied. Fractional deviations for energy deposition averaged 1 percent close to the burst and about 6 percent near the 3-km boundary.

It was observed that energy deposition from outgoing gamma rays was about eight times that from backscattered incoming gamma rays, at any range in the air. The backscatter from the ground was much less, so that radial Compton current and energy deposition were weaker near the ground and the theta Compton current was strongest. This effect is clear since gamma rays must flow from the air into the ground and be attenuated there; this flow causes a negative gradient in the flux close to the ground. From a different viewpoint, the buildup factor is reduced near the ground.

Since effects due to multiply scattered gamma rays come later in time than effects due to unscattered gamma rays, the time dependence of effects was confirmed to be range dependent. At deeper penetrations, the buildup factor is greater so that multiply scattered effects are stronger. The result is that the energy deposition decay rate in time is slower at deeper penetrations. The ratio of radial Compton current to energy deposition rate also declines with time more slowly with increasing range. In fact, the time dependence of the latter ratio roughly scales as the inverse of the buildup factor (that is, scaled time t' \approx tB).

A similar SLEDGE run was done for a 0.5-MeV gamma ray source. Results of both runs were stored on magnetic tape for subsequent analysis.

PART II. ANALYTICAL FITS TO EMP DRIVER RESULTS

4. ENERGY DEPOSITION

4.1 Fitting Free-Field Buildup Factors for Seven Gamma Ray Energies

Seven gamma ray energies from 0.5 to 7.0 MeV (table 1) were chosen to allow flexibility in representing approximately an arbitrary nuclear burst gamma ray energy spectrum. Since gamma-induced EMP sources may contribute to EMP generation at distances as great as about 5 km, the gamma ray transport was carried to a range of 25 attenuation lengths to ascertain the true range dependence of the buildup factor for energy deposition. Based on theory, a reasonable approximation to the buildup factor is given by

$$B(r) = 1 + a(r/\lambda)^{k},$$

where $\boldsymbol{\lambda}$ is the attenuation length and $\,$ a $\,$ may be shown by energy conservation to be

$$a = \mu_S / [\mu_a \Gamma(k+1)] ,$$

where

 μ_s = total scattering coefficient ($\mu_s = \sigma_s + 1.022\sigma_{pp}/E$),

σ_e = Compton scattering coefficient,

 σ_{pp} = pair production attenuation coefficient,

E = gamma ray energy in MeV,

 μ_a = total absorption coefficient for Compton absorption, photoabsorption, and pair production $\left[\mu_a = \sigma_a + \sigma_{ph} + \sigma_{pp}(2 - 1.022)/E\right],$

σ_a = Compton absorption coefficient,

 σ_{ph} = photoabsorption attenuation coefficient,

 $\Gamma(k+1) = gamma function of k+1,$

k = function of (source) gamma ray energy.

Parameter k is of order unity and is the only free quantity in the expression for B.

The expression for B was fitted, by adjustment of k, to the 1-d detector results obtained by the SLEDGE code. Twenty-five detectors were used, each one attenuation length thick. The least-squares fit was

obtained by minimizing the sum of the squares of the errors over all detectors, with each square weighted by the reciprocal of the square of the fractional deviation for the detector. Buildup factor parameters a and k so obtained are given in table 3 for each gamma ray energy. The buildup factor predicted by these values of a and k has a probable error of not more than 1 percent due to the uncertainty in the Monte Carlo data. Although the fractional deviation for the detectors varies from about 3 to about 10 percent, the combined fractional deviation (of all 25 detectors fitted at once) is less than 1 percent. However, this 1-percent error estimate does not include the possibility of systematic

error due to the true buildup factor not being perfectly represented by the expression $1+a(r/\lambda)^k$. This error estimate does describe how closely the a and k parameter values, thus obtained by fitting Monte Carlo data, approximate the best fit of the expression to the true buildup factor.

As to possible systematic error, it appears that the fit may be low by about an average 2 percent to 10 attenuation lengths range, but this level remains uncertain because of the size of statistical error of the Monte Carlo data. Statistical error at farther ranges is even greater and permits no assessment of systematic error.

TABLE 3. ENERGY DEPOSITION BUILDUP FACTOR PARAMETERS FOR $B = 1 + a(r/\lambda)^k$

Source gamma ray energy (MeV)	a	k
0.5	1.534	1.418
1.0	1.162	1.188
1.5	0.960	1.143
2.5	0.800	0.976
3.5	0.695	0.903
5.0	0.580	0.880
7.0	0.473	0.891

4.2 Ground Effect on Buildup Factor

Analysis of the 2-d detector results of the two SLEDGE runs, for 0.5- and 1.5-MeV gamma ray point sources at 200 m aboveground, showed a distinct depletion of energy deposition near the ground. An exception is that early energy deposition is enhanced beneath the burst due to immediate backscatter from the ground. However, this effect will be neglected in the following development since EMP in this region is not important to typical Army electronic systems because of overwhelming blast and thermal damage.

For observers near the ground and for a range such that the line of sight to the burst is shallow, the buildup factor was limited in its growth. This limitation was interpreted that the ground (although

flat) introduced an effective horizon because the ground intercepts multiply scattered gamma rays that would otherwise contribute. The effective horizon, H, is approximately

$$H = 3.0r/(9.0 + r^2/\lambda^2)^{1/2}$$

for horizontal gamma ray incidence near the ground.

The effective horizon for horizontal incidence, h, at height z aboveground is approximately

$$h = He^{z/\lambda}$$
.

For incidence at angle θ to the horizontal, the effective horizon at the observer will be approximated by the averaging integral

$$h = \int_0^H e^{z(r)/\lambda} dr = \int_0^H e^{[r(\sin\theta)+Z]/\lambda} dr ,$$

or

$$h = \frac{\lambda e^{Z/\lambda}}{\sin \theta} \left[e^{H(\sin \theta)/\lambda} - 1 \right] ,$$

where z(r) is the height at range r on the line of sight from the burst to the observer and Z is the observer height aboveground.

The ground-influenced buildup factor, $\hat{B}(R,Z)$, a function of observer range and height, is asymptotically limited to B(h), that attained within effective horizon h. Based on the SLEDGE 2-d results, a good approximation for the ground-influenced buildup factor is

$$\hat{B}(R,Z) = (1/2)[B(r) + X]$$

where B(r) is the free-field buildup factor for range r from the source and

$$X = 1 + 1/(1/[B(r) - 1]^2 + 1/\{4 + [B(h) - 1]^2\})^{1/2}.$$

4.3 Time Dependence of Energy Deposition Rate

The time-dependent energy deposition rate, S, at distance r, height z, and time t contributed by multiply scattered gamma rays (that is, excluding uncollided gamma rays) from a delta-function (in time) point gamma source of one gamma of energy, E, is written as

$$S(r,z,t) = U(r)N(r,z)T(r,z,t) ,$$

where

U(r) = energy deposition from uncollided gamma ray number
flux (that is, first-scatter deposition),

N(r,z) = normalization factor (including buildup factor),

T(r,z,t) = explicit time dependence.

U(r) is given by

$$U(r) = Ee^{-r/\lambda}/\left(4\pi r^2\lambda_{abs}\right),$$

where E is the gamma ray energy, λ is the attenuation length, and λ_{abs} is the absorption length. Based on the 1.5-MeV gamma ray source SLEDGE results, a good approximation for T is

$$T(r,z,t) = (t + t_0)^m e^{-pt} ,$$

where

$$t_0 = 10^8 \text{ s},$$
 $m = -1/[1 + f(r,z)r/\lambda],$
 $p = 1.4 \times 10^6 \text{ s}^{-1}.$

Function f(r,z) is described later.

We require S to be independent of z at t=0 since the ground affects only multiply scattered gamma rays (for an observer aboveground), and these gamma rays always arrive after t=0. We require also the following normalization:

$$\int_0^\infty S(r,z,t) dt = U(r)[\hat{B}(r,z) - 1],$$

where \hat{B} is the ground-influenced buildup factor. For $z=\infty$, \hat{B} becomes free-field buildup factor B(r). From this normalization, we obtain

$$N(r,z) \int_0^\infty T(r,z,t) dt = \hat{B}(r,z) - 1.$$

Let I be defined as the integral

$$I = \int_0^\infty T(r,z,t) dt$$
$$= \int_0^\infty (t + t_0)^m e^{-pt} dt .$$

By straightforward means, the integral is found to be

$$I = e^{pt_0} p^{-\epsilon} \Gamma(\epsilon) [1 - P(\epsilon, pt_0)],$$

where

 $\varepsilon = 1 + m$,

 $\Gamma(\varepsilon)$ = gamma function of ε ,

 $P(\varepsilon, pt_0)$ = incomplete gamma function.⁵

Hence, normalization factor N(r,z) is

$$N(r,z) = [\hat{B}(r,z) - 1]/I.$$

Since function f(r,z) has not been specified yet, variable ϵ ,

$$\varepsilon = 1 - 1/[1 + f(r,z)r/\lambda] ,$$

remains unconstrained. We use it to satisfy the requirement that S(r,z,t) be independent of z at t=0. At earliest times, the transport is essentially free field, so free-field data far from the ground should describe the t=0 transport. By examination of SLEDGE data for detectors far from the ground (virtually free field), it was determined that a value f=0.2 would cause S to fit these data reasonably well. This value is called f_{∞} (that is, $f_{\infty}\equiv0.2$). Let the corresponding value for ε be

$$\varepsilon_{\infty}$$
 = 1 - 1/(1 + $f_{\infty}r/\lambda$) .

We require the transport near the ground at t=0, to be the same as the transport far $(z \to \infty)$ from the ground, also at t=0. Thus,

$$S(r,z=\infty,t=0) \equiv S(r,z,t=0)$$
,

or

$$\frac{[B(r) - 1]T(r,z=\infty,t=0)}{I(r,z=\infty)} = \frac{\left[\hat{B}(r,z) - 1\right]T(r,z,t=0)}{I(r,z)}.$$

This can be expanded to

$$\frac{[B(r) - 1]t_0^{\varepsilon_{\infty}-1}}{e^{pt_0 - \varepsilon_{\infty}} \Gamma(\varepsilon_{\infty})[1 - P(\varepsilon_{\infty}, pt_0)]} = \frac{\left[\hat{B}(r,z) - 1\right]t_0^{\varepsilon-1}}{e^{pt_0 - \varepsilon} \Gamma(\varepsilon)[1 - P(\varepsilon, pt_0)]},$$

⁵Milton Abramowitz and Irene Stegun, Handbook of Mathematical Functions, Dover Publications, Inc., New York (1965), 260.

where ε is a function of z. If we define $G(\varepsilon)$ by

$$G(\varepsilon) = t_0^{1-\varepsilon} e^{pt_0} p^{-\varepsilon} \Gamma(\varepsilon) [1 - P(\varepsilon, pt_0)] ,$$

then this may be written

$$[B(r) - 1]/G(\varepsilon_{\infty}) = [\hat{B}(r,z) - 1]/G(\varepsilon)],$$

or

$$G(\varepsilon) = G(\varepsilon_{\infty})[\hat{B}(r,z) - 1]/[B(r) - 1]$$
.

Thus, given r and z, $G(\varepsilon)$ may be determined from $G(\varepsilon_{\infty})$, B(r), and $\hat{B}(r,z)$. $G(\varepsilon)$ may then be inverted to yield ε . Having ε and $m=\varepsilon-1$, one may obtain

$$I = G(\varepsilon)t_0^m,$$

$$N(r,z) = \left[\hat{B}(r,z) - 1\right]/I,$$

$$T(r,z,t) = \left(t + t_0\right)^m e^{-pt},$$

$$S(r,z,t) = U(r)N(r,z)T(r,z,t).$$

Inverting $G(\epsilon)$ for ϵ involves tabulating G for a large number of values of ϵ and then using a table-lookup algorithm to get ϵ from G.

By using the approach just described, the energy deposition rate may be obtained for any r,z,t in such a way that it evolves in time from an initial free-field distribution to a progressively more ground-influenced distribution. Time integrals of the energy deposition rate are correctly normalized to expected ground-influenced buildup factors.

These results are scaled to first order to source gamma ray energies other than 1.5 MeV by geometrically scaling r, z, and t by the attenuation length. This is already built into buildup factors B and \hat{B} and variable m (and ϵ). Only the time remains to be scaled. If subscript "1.5" denotes 1.5-MeV source gamma rays and if

$$\alpha \equiv \lambda_{1.5}/\lambda(E)$$
,

where $\lambda(E)$ is the attenuation length for gamma ray energy E, then

$$G(\varepsilon) = (\alpha t_0)^{1-\varepsilon} e^{p\alpha t_0} p^{-\varepsilon} \Gamma(\varepsilon) [1 - P(\varepsilon, p\alpha t_0)],$$

$$I = G(\varepsilon) (\alpha t_0)^m / \alpha,$$

$$T(r, z, t) = (\alpha t + \alpha t_0)^m e^{-p\alpha t}.$$

Variable m is evaluated for $\lambda = \lambda(E)$ as

$$m = - 1/[1 + fr/\lambda(E)] .$$

The uncollided energy deposition, U, becomes

$$U(r) = Ee^{-r/\lambda(E)}/[4\pi r^2 \lambda_{abs}(E)] .$$

5. RELATION OF COMPTON CURRENT TO ENERGY DEPOSITION RATE

5.1 Compton Current from First Collisions of Gamma Rays

For point source gamma rays experiencing their first collision in air having density 1.11 kg/m 3 , the radial Compton current produced is simply related to the corresponding energy deposition:

$$J_r/S = k_0(E) .$$

The theta Compton current, J_{θ} , is identically zero for first scatters. Factor $k_{0}(E)$ is given in table 4 for the seven gamma ray energies considered. The values are based on estimates of the mean forward range of Compton electrons, including multiple scattering of the Compton electrons as well. Factor $k_{0}(E)$ equals $\lambda_{a}R_{c}/(\rho\lambda_{c}E)$, where λ_{a} and λ_{c} are the Compton absorption and collision lengths, ρ is the air density, R_{c} is the mean forward range of the Compton electrons, and E is the gamma ray energy.

TABLE 4. RATIO OF RADIAL COMPTON ELECTRON
CURRENT TO ENERGY DEPOSITION FOR
FIRST-COLLISION GAMMA RAYS FROM
A POINT SOURCE

Source gamma ray energy (MeV)	Ratio k ₍ (E) (electron-m/MeV)
0.5	1.061
1.0	1.606
1.5	1.952
2.5	2.338
3.5	2.508
5.0	2.561
7.0	2.454
7.0	2.454

⁶William T. Wyatt, Jr., Transmission Factor Effects on the Average Forward Range of Compton Electrons, Harry Diamond Laboratories HDL-TM-80-10 (January 1980).

5.2 Radial Compton Current from Multiply Scattered Gamma Rays

For multiply scattered gamma rays, the radial Compton current produced is related to the corresponding energy deposition by

$$J_r/S = k(r,t,E)$$
,

where r is the distance from the point source of gamma rays and t is retarded time. The SLEDGE 1-d results for each of the seven gamma ray energies can be fitted by

$$k(r,t,E) \approx k_0(E)(0.91 + 0.03E^{1/2})e^{-T}$$
,

where

$$T = \frac{1.0 \times 10^{-8} p_1 (1.0 \times 10^{8} t)^{P_2}}{[B(R) - 1]^{P_4}}$$

and

$$R = r + \lambda (p_3 + p_5 t/[r/\lambda]^{p_6}) .$$

Factor $k_0(E)$ is defined in section 5.1. Buildup factor B is evaluated for modified range R. Optimum fit values for p_1 , p_2 , p_3 , p_4 , p_5 , and p_6 are listed in table 5 for the seven gamma ray energies.

TABLE 5. FIT PARAMETERS FOR RATIO OF RADIAL COMPTON ELECTRON CURRENT TO ENERGY DEPOSITION RATE FOR MULTIPLY SCATTERED GAMMA RAYS

energy (MeV)	Pl	P ₂	P ₃	P ₄	P ₅	P ₆
0.5	3.880(7) ^a	1.384	7.599(-2)	0.855	2.793(7)	-0.0847
1.0	1.783(7)	1.040	1.304(-1)	0.685	0.817(7)	+0.0524
1.5	1.162(7)	1.025	7.358(-2)	0.596	0.537(7)	-0.1179
2.5	0.964(7)	0.974	1.765(-2)	0.679	0.339(7)	+0.0605
3.5	0.769(7)	0.974	1.679(-2)	0.758	0.247(7)	+0.1410
5.0	0.358(7)	1.230	7.253(-2)	0.947	0.523(7)	-0.1091
7.0	0.835(6)	1.865	7.869(-2)	1.561	1.336(7)	-0.0886

^aRead as 3.880 \times 10⁷.

Quantity k(r,t,E) decays more slowly with increasing range. Also, in theory one would expect k at time t=0 to be exactly $k_0(E)$ since the earliest scattered gamma rays to arrive at any point are those that have experienced a single grazing scatter and thus have nearly the same energy, E. However, the Monte Carlo studies show that

$$k(r,t,E) \approx k_0(E)(0.91 + 0.03E^{1/2})$$

when averaged over the first time bin, which is 5 ns wide. This resolution of the time history appears to be adequate since most gamma ray output from a nuclear burst is emitted over about 10 ns.

5.3 Theta Compton Current from Multiply Scattered Gamma Rays

The theta Compton current from a point gamma ray source near the earth is secondary to the radial Compton current in magnitude and in efficiency as a generator of EMP. In the SLEDGE 2-d results, variance was larger for the theta current component—often so large that the sign of the component was doubtful. Nevertheless, some significant trends were clearly observed at late times near the ground. The ratio of theta Compton current to energy deposition rate (for an air density of 1.11 kg/m^3) is approximately

$$J_{A}/S = 1.5 \times 10^{5} te^{-0.02z}$$

where t is retarded time in seconds and z is height aboveground in meters. Thus, the theta component is strongest near the ground and decays (about) exponentially with increasing height.

This expression for J_{θ}/S is not strongly dependent upon source gamma ray energy to a first approximation since the late-time currents derive from low-energy multiply scattered gamma rays.

6. COMPARISON WITH PREVIOUS RESULTS

6.1 Buildup Factor for Energy Deposition

The LEMP code prompt gamma ray drivers (H. J. Longley, Mission Research Corp.) include buildup factor curve fits for energy deposition and radial Compton current for three source gamma ray energies (0.5, 1.5, and 5.0 MeV). No account is taken of the influence of the ground. The energy deposition buildup factor obtained for air was based on published data for water.

Recently, Malik, Cashwell, and Schrandt⁷ at the Los Alamos Scientific Laboratory (LASL) obtained curve fits to buildup factors and

⁷J. S. Malik, E. D. Cashwell, and R. G. Schrandt, The Time Dependence of the Compton Current and Energy Deposition from Scattered Gamma Rays, Los Alamos Scientific Laboratory, NM, LA-7386-MS (July 1978).

time dependence of energy deposition and Compton current from scattered gamma rays in homogeneous isotropic air. These curve fits to their Monte Carlo data were obtained for gamma ray energies of 1, 1.5, 2, 3, 4, and 6 MeV to a range of 1600 m. Air density was 1.1 mg/cm^3 .

The LEMP and LASL buildup factors are compared with NEMP freefield and ground-influenced buildup factors (for energy deposition) in figures 1 to 6. The NEMP ground-influenced buildup factor is for a burst and an observer both at a 0-m height aboveground. Figures 1 to 3 show results as a function of range in units of attenuation lengths, from 0 to 25 attenuation lengths. These results exclude the effect of any disagreement in attenuation length among the LEMP, LASL, and NEMP drivers and compare directly the functional forms used. Figures 1 to 3 show, respectively, 0.5-, 1.5-, and 5.0-MeV source gamma ray buildup The 0.5-MeV energy is below the 1.0-MeV lower limit for the factors. LASL transport data and shows that the LASL drivers are in substantial error below the designated range. The LEMP and NEMP curves are in good agreement to about four attenuation lengths range, after which the LEMP curve is higher. For 0.5 MeV, the disagreement becomes very large. quality of agreement between LEMP and NEMP at closer ranges, however, tends to confirm their validity at such ranges. The LASL curves, on the other hand, seem too low except for the 5.0-MeV results (fig. 3). The low-energy disagreement among LEMP, NEMP, and LASL is ameliorated by the fact that, for a realistic gamma ray energy spectrum, higher energy gamma rays predominate at substantial ranges because of their greater penetrating ability.

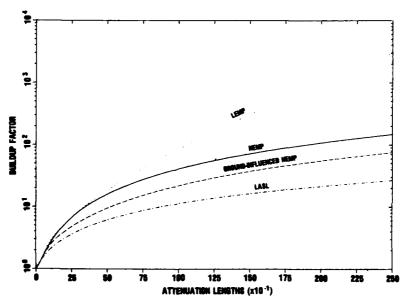


Figure 1. Energy deposition buildup factors compared for 0.5-MeV gamma rays, for range in attenuation lengths.

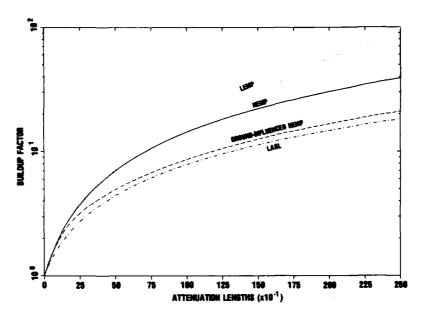


Figure 2. Energy deposition buildup factors compared for 1.5-MeV gamma rays, for range in attenuation lengths.

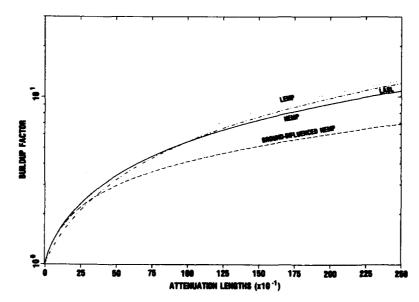


Figure 3. Energy deposition buildup factors compared for 5.0-MeV gamma rays, for range in attenuation lengths.

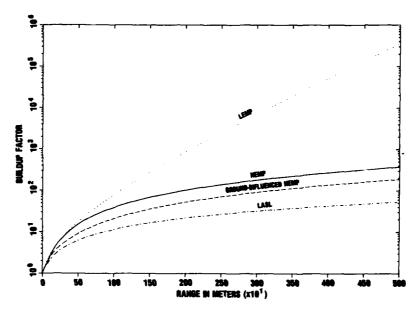


Figure 4. Energy deposition buildup factors compared for 0.5-MeV gamma rays, for range in meters.

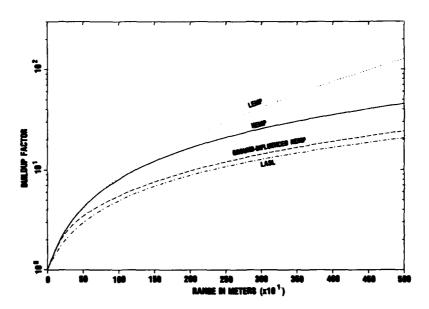


Figure 5. Energy deposition buildup factors compared for 1.5-MeV gamma rays, for range in meters.

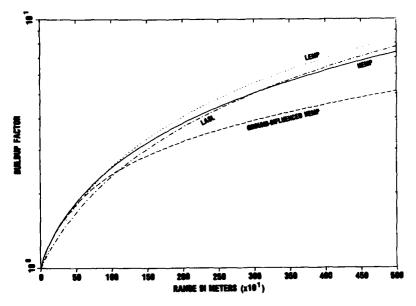


Figure 6. Energy deposition buildup factors compared for 5.0-MeV gamma rays, for range in meters.

Figures 4 to 6 include the attenuation length, but still appear similar to figures 1 to 3. Careful comparison of SLEDGE transport results with the NEMP curve fit shows that the NEMP curve fit is about 10 percent higher over the first attenuation length. But the NEMP curve fit is found to be accurate to a few percent at greater ranges.

The NEMP ground-influenced buildup factor in figures 1 to 6 is as much a factor of two smaller than the corresponding NEMP free-field buildup factor. The difference increases monotonically with range, more slowly for more energetic gamma rays, to a difference of as much as a factor of two.

6.2 Time Dependence of Energy Deposition Rate

The time dependence of the free-field NEMP, LEMP, and LASL energy deposition rate drivers is shown in figures 7 to 12 for three source gamma ray energies (0.5, 1.5, and 5.0 MeV) and two ranges from the burst (300 and 3000 m). The three curves are normalized to a time integral of unity, removing any disagreement in attenuation length and buildup factor. A fourth curve represents the ground-influenced NEMP energy deposition rate for burst and observer on the ground. This curve is normalized to the free-field case, so the difference between this curve and the free-field NEMP curve is a diminution of the energy deposition rate due to the presence of the ground.

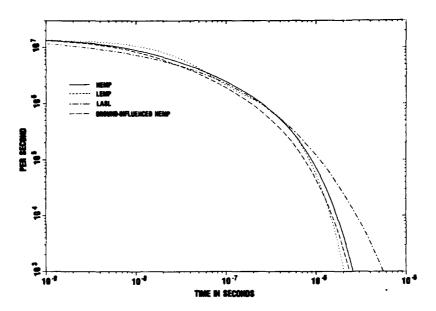


Figure 7. Time dependence of energy deposition buildup factors compared at 300-m range for 0.5-MeV gamma rays.

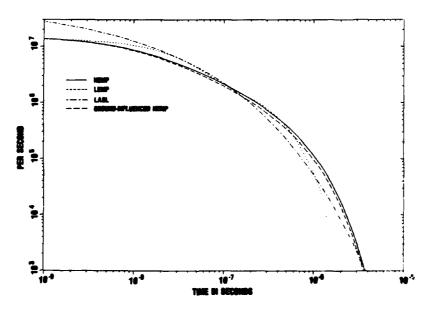


Figure 8. Time dependence of energy deposition buildup factors compared at 300-m range for 1.5-MeV gamma rays.

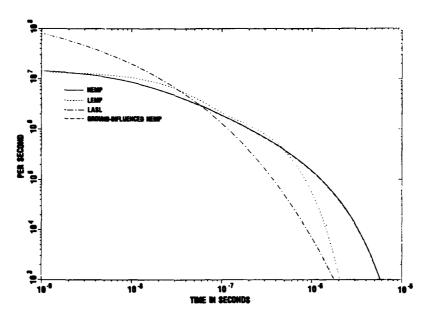


Figure 9. Time dependence of energy deposition buildup factors compared at 300-m range for 5.0-MeV gamma rays.

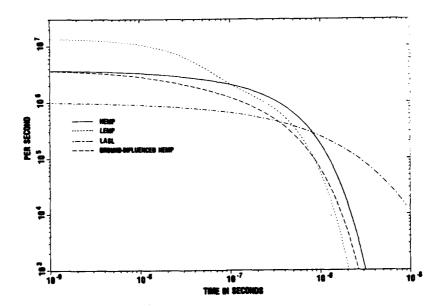


Figure 10. Time dependence of energy deposition buildup factors compared at 3000-m range for 0.5 MeV-gamma rays.

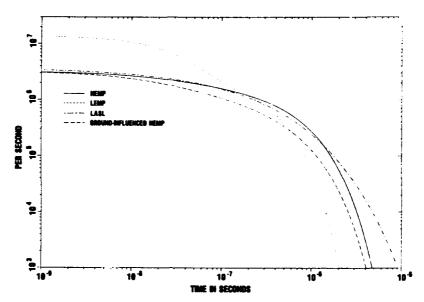


Figure 11. Time dependence of energy deposition buildup factors compared at 3000-m range for 1.5-MeV gamma rays.

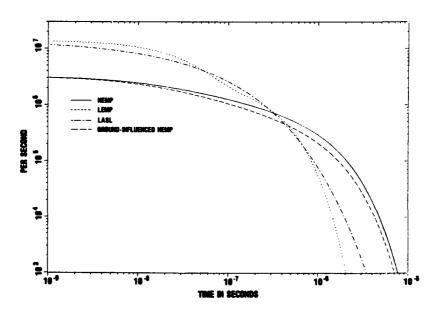


Figure 12. Time dependence of energy deposition buildup factors compared at 3000-m range for 5.0-MeV gamma rays.

Figures 7 to 9 show the energy deposition rate at a 300-m range for 0.5-, 1.5-, and 5.0-MeV source gamma ray energies. The agreement between the NEMP and LEMP drivers is good. Since the LEMP driver was based on close-in data, we expect it to be accurate at a 300-m range. The extremely close agreement at 1-ns retarded time is particularly encouraging and tends to confirm the correctness of the first-scatter part of the NEMP driver. The LASL curve seems to be concentrated too much toward early times, except for the 0.5-MeV curve.

Figures 10 to 12 show the energy deposition rate at a 3000-m range for 0.5-, 1.5-, and 5.0-MeV source gamma ray energies. At this deep penetration, we expect the LEMP curves to be concentrated too much toward early times in comparison with the NEMP curve--and they are. The NEMP and LASL curves agree well only for 1.5 MeV (fig. 11). For 5.0 MeV (fig. 12), the LASL curve is too close to the LEMP curve. Data shown in the LASL report⁷ confirm a tendency of that curve fit to overestimate the energy deposition rate earlier than a fraction of a microsecond, for deep penetrations of about 10 attenuation lengths.

In all figures shown, the NEMP ground-influenced energy deposition rate begins equal to the NEMP free-field curve and later falls below by as much as a factor of about three for the 3000-m curve. For the 300-m curve, little difference is noted.

6.3 <u>Time Dependence of Radial Compton Current</u>

The ratio of radial Compton electron current to energy deposition rate is shown as a function of time for the NEMP, LEMP, and LASL drivers in figures 13 to 18. Figures 13 to 15 are for gamma ray energies of 0.5, 1.5, and 5.0 MeV at a range of 300 m from the burst. Figures 16 to 18 are for the same gamma ray energies at a range of 3000 m. The units of the ratios plotted are in Compton electron-meter per MeV. A factor of 0.8 has been separately applied to the LEMP and LASL drivers to account for multiple scattering of Compton electrons. effect is already included in the NEMP driver. As for energy deposition rate, we expect the LEMP data to be more accurate at 300 m than at 3000 m. Good agreement is observed among all three curves (NEMP, LEMP, and LASL) at 300 m for each gamma ray energy, with a few exceptions. NEMP curve is probably too high after about 1 μs , although the significance of the discrepancy is slight in terms of the EMP that would be Also, the LASL early time value for 0.5 MeV is high by more produced. than a factor of two.

⁷J. S. Malik, E. D. Cashwell, and R. G. Schrandt, The Time Dependence of the Compton Current and Energy Deposition from Scattered Gamma Rays, Los Alamos Scientific Laboratory, NM, LA-7386-MS (July 1978).

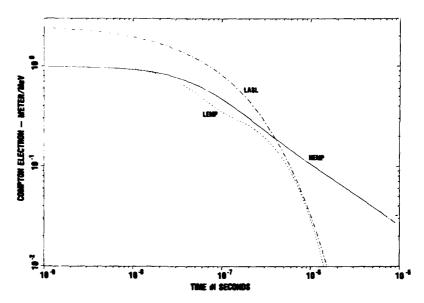


Figure 13. Time dependence compared for ratio of radial Compton electron current to energy deposition rate, at 300-m range for 0.5-MeV gamma rays.

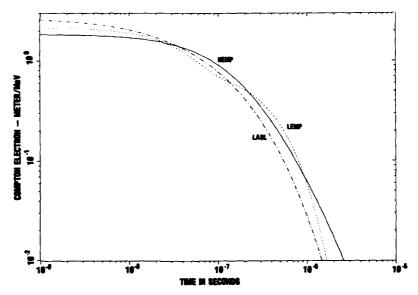


Figure 14. Time dependence compared for ratio of radial Compton electron current to energy deposition rate, at 300-m range for 1.5-MeV gamma rays.

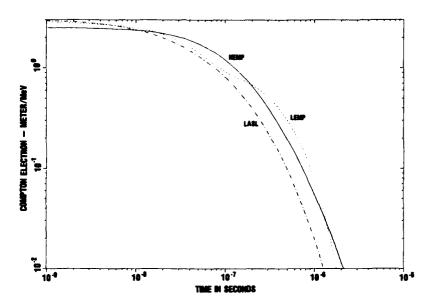


Figure 15. Time dependence compared for ratio of radial Compton electron current to energy deposition rate, at 300-m range for 5.0-MeV gamma rays.

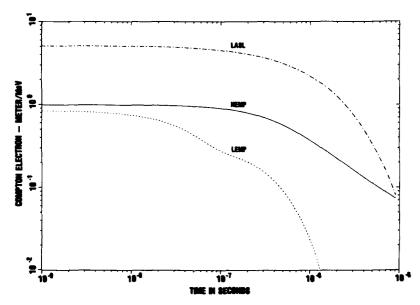


Figure 16. Time dependence compared for ratio of radial Compton electron current to energy deposition rate, at 3000-m range for 0.5-MeV gamma rays.

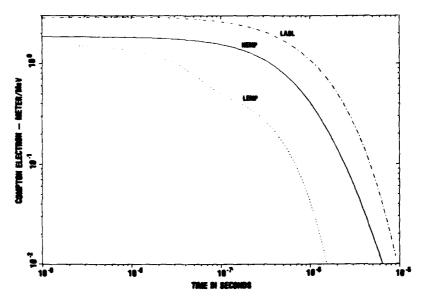


Figure 17. Time dependence compared for ratio of radial Compton electron current to energy deposition rate, at 3000-m range for 1.5-MeV gamma rays.

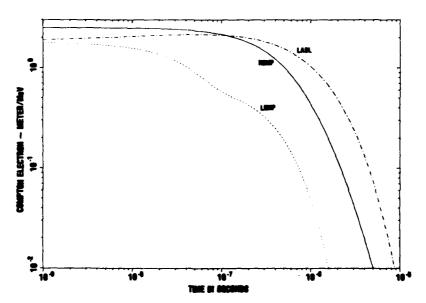


Figure 18. Time dependence compared for ratio of radial Compton electron current to energy deposition rate, at 3000-m range for 5.0-MeV gamma rays.

Agreement is worse at 3000 m for each gamma ray energy. The NEMP and LEMP curves are in fair agreement at early times, whereas the LASL curve is too high except for the 5.0-MeV curve. The LEMP curve decays much too fast, as expected at deep penetration where multiply scattered gamma rays retain more of their collimation than at shallow penetration. (The LEMP driver is based on shallow penetration data). The LASL curve, on the other hand, decays too slowly. Comparison of the NEMP curves with the Monte Carlo data that they were intended to fit reveals that the curves are usually somewhat too high after about 1 μs , up to a factor of about two. However, considering the steepness of the curve, this error is not serious. No doubt a more complicated functional form would approximate the Monte Carlo data more faithfully.

From these comparisons, LEMP drivers would underestimate the Compton current at 3000 m by about a factor of four at 100 ns after the gamma-dot peak, for any of the gamma ray energies considered. The LASL drivers should not be applied to gamma ray energies less than 1.0 MeV, and they also significantly overestimate the Compton current at 3000 m for 1.5 MeV.

No ground effect on the ratio of Compton current to energy deposition rate was identified.

7. CONCLUDING REMARKS

This report presents improved calculations of EMP drivers due to a gamma ray point source in air over ground and analytic approximations to these EMP drivers. These were done for seven source gamma ray energies from 0.5 to 7.0 MeV. The EMP driver calculations were based on Monte Carlo simulation of the gamma ray transport using the SLEDGE computer code developed for this study. Notable features of the simulation included tracking to 25 attenuation lengths (mean free paths) penetration, presence of the earth, use of correlated sampling to estimate Compton electron currents more accurately, and extensive use of biasing and importance functions. The theoretical basis of the SLEDGE code is discussed. Significant aspects of the Monte Carlo results also are discussed.

The analytic approximations to the EMP drivers are described in detail, including (1) the energy deposition buildup factor (both free field and ground influenced), (2) time dependence of energy deposition as a function of both range from the burst and nearness to the ground, (3) ratio of radial Compton electron current to energy deposition rate, and (4) theta Compton electron current due to the presence of the ground. These approximations have been incorporated into an EMP driver software package used with the NEMP near-surface-burst EMP environment prediction code. Comparisons are made with two previous EMP driver

packages, one used in the LEMP surface-burst EMP environment prediction code and the other originated by LASL scientists for high-altitude burst problems. Free-field agreement with the LEMP drivers was generally good at short ranges. Free-field agreement with the LASL drivers was better at higher gamma ray energies. The new results predict ground effects as well, which were not considered by the LEMP and LASL researchers.

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